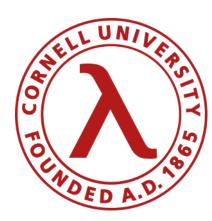


Automated Differential Testing for OCaml Modules

Ernest Ng
Harry Goldstein
Benjamin Pierce









A module signature for sets

```
module type S = sig
  type 'a t
  val empty : 'a t
  val insert : 'a → 'a t → 'a t
  ...
end
```

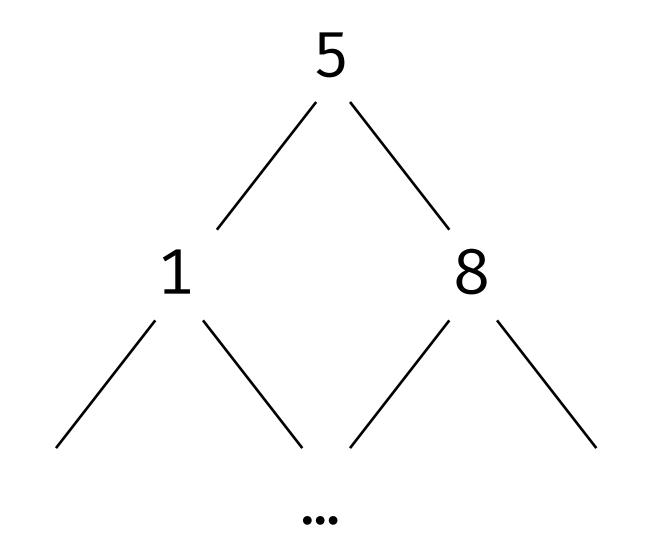
module type S

```
module type S
```

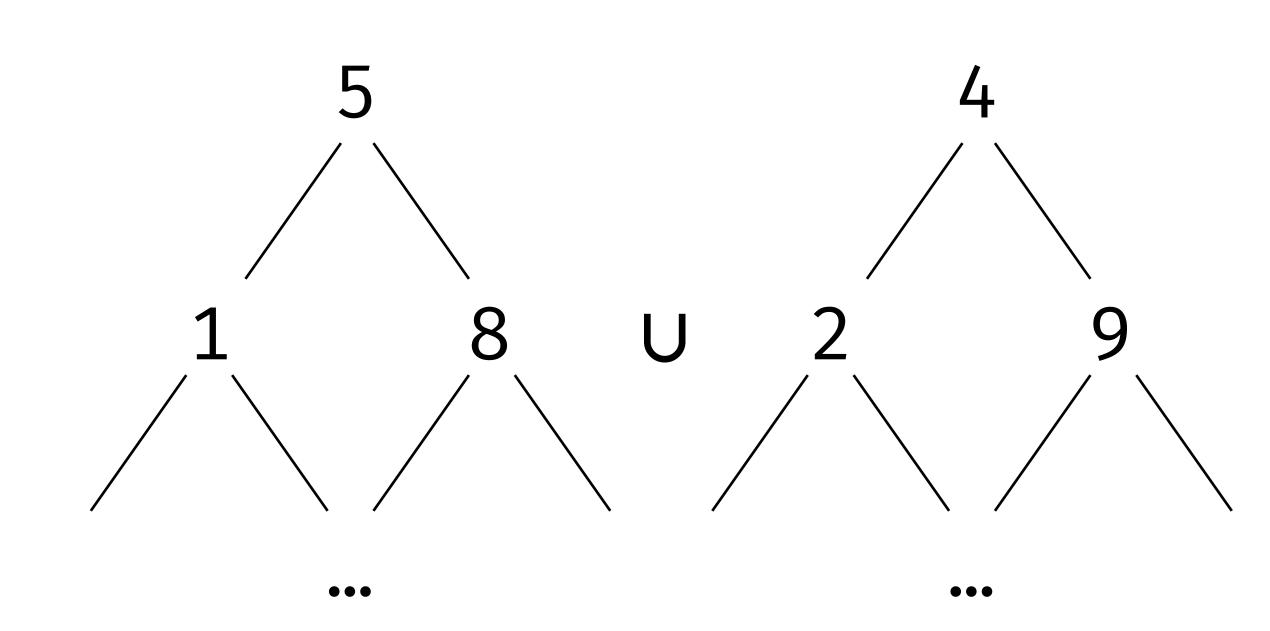
module ListSet : S

```
module type S
```

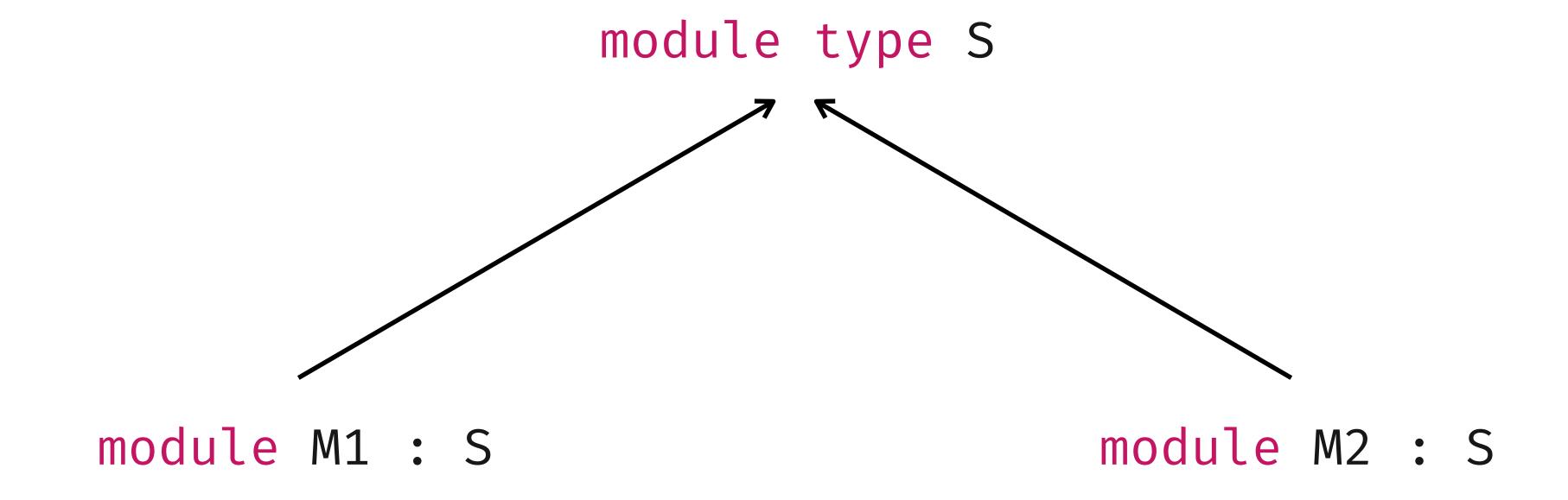
module BSTSet : S



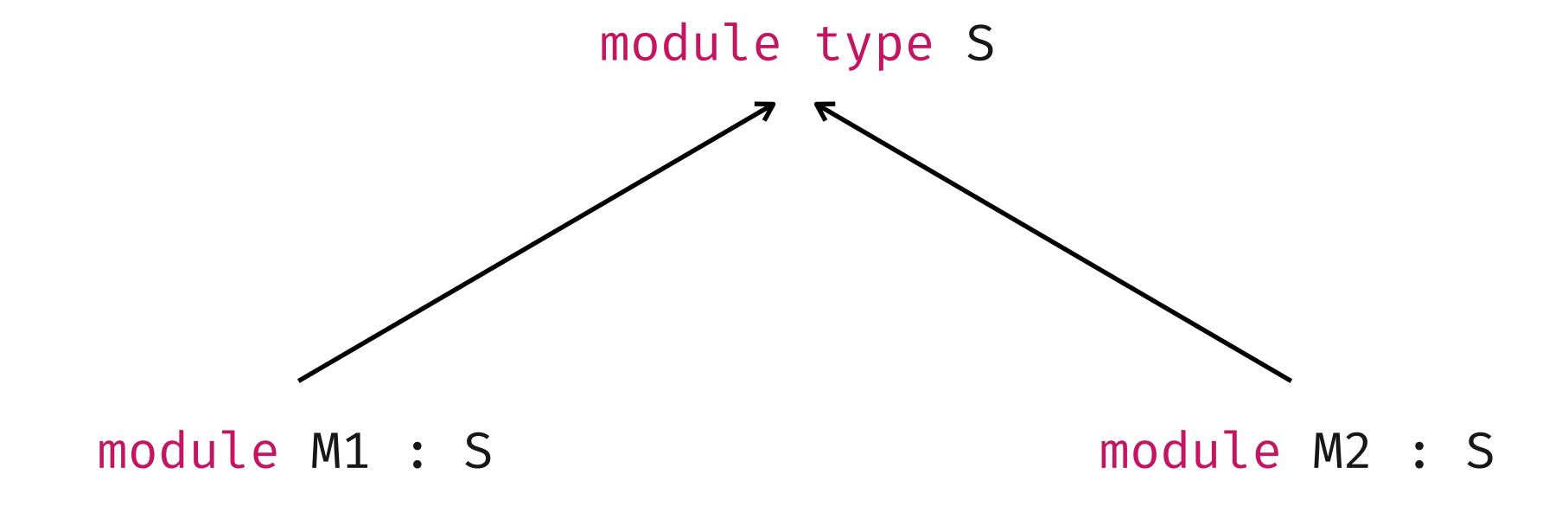
Are these equivalent?



Two modules can implement the same interface completely differently ...

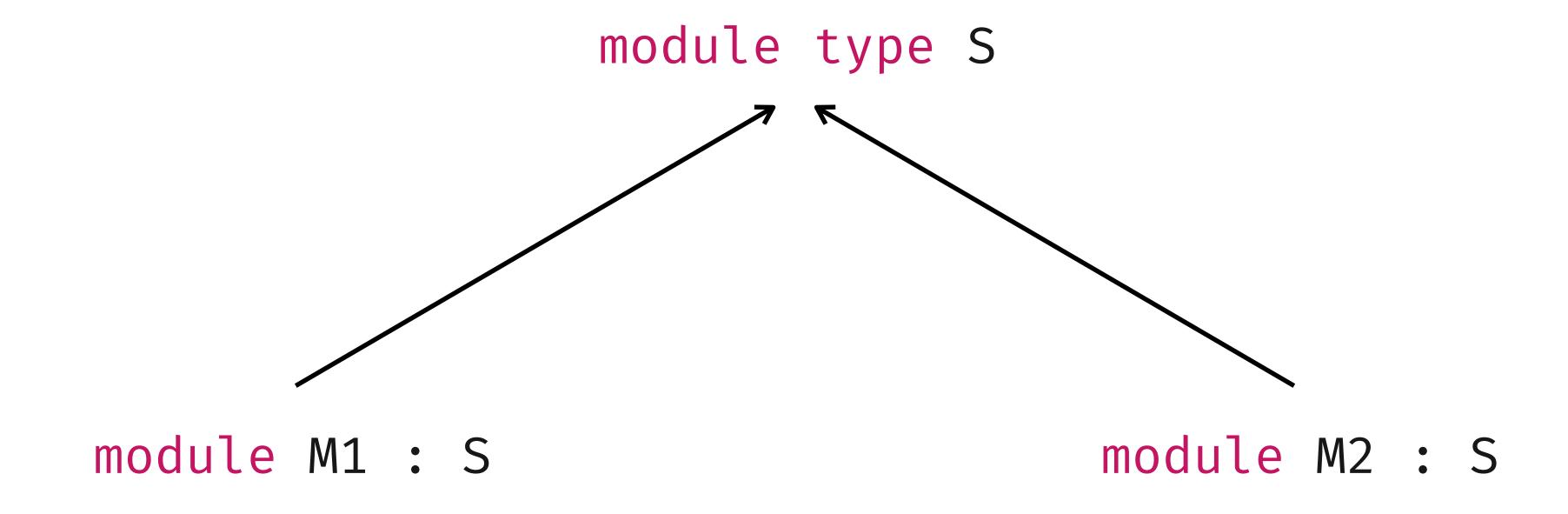


Two modules can implement the same interface completely differently ...



Clients can use S without knowing whether they're getting M1 or M2!

Two modules can implement the same interface completely differently ...

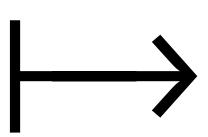


Clients can use S without knowing whether they're getting M1 or M2!

Both modules ought to behave <u>equivalently</u> w.r.t. the same interface!

Observational Equivalence

equivalent inputs



equivalent outputs

How do we check observational equivalence?

How do we check observational equivalence?

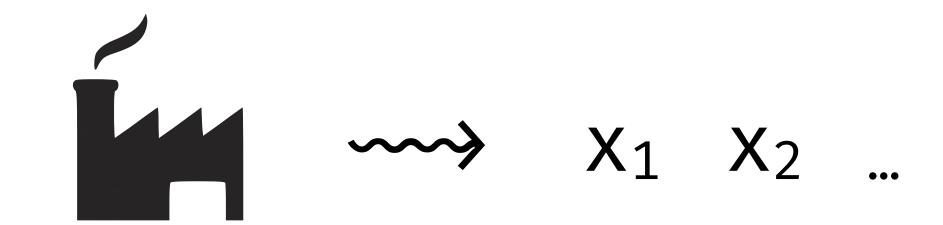
We can use property-based testing!

1. Write properties

$$\forall x. P(x)$$

$$\forall x. P(x)$$

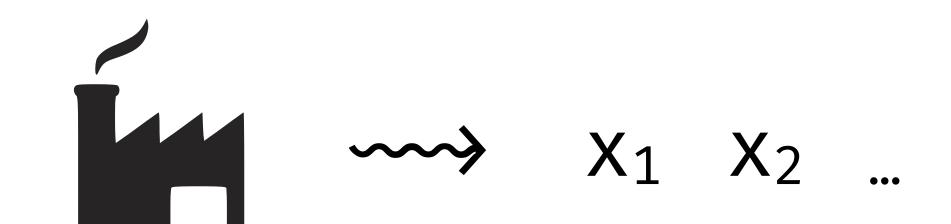
1. Write properties 2. Generate random inputs



1. Write properties

$$\forall x. P(x)$$

2. Generate random inputs



3. Check if inputs satisfy property



Popularized by:

QuickCheck

Claessen & Hughes (ICFP 2000)

Why should we care?

1. Testing observational equivalence requires significant programmer effort

Goldstein et al. (ICSE '24)

Property-Based Testing in Practice

Harrison Goldstein

University of Pennsylvania Philadelphia, PA, USA hgo@seas.upenn.edu

Joseph W. Cutler

University of Pennsylvania Philadelphia, PA, USA jwc@seas.upenn.edu

Daniel Dickstein

Jane Street New York, NY, USA ddickstein@janestreet.com

Benjamin C. Pierce

University of Pennsylvania Philadelphia, PA, USA bcpierce@seas.upenn.edu

ABSTRACT

Property-based testing (PBT) is a testing methodology where users write executable formal specifications of software components and an automated harness checks these specifications against many automatically generated inputs. From its roots in the QuickCheck library in Haskell, PBT has made significant inroads in mainstream languages and industrial practice at companies such as Amazon.

Andrew Head

University of Pennsylvania Philadelphia, PA, USA head@seas.upenn.edu

The research literature is full of accounts of PBT successes, e.g., in telecommunications software [2], replicated file [31] and key-value [8] stores, automotive software [3], and other complex systems [30]. PBT libraries are available in most major programming languages, and some now have significant user communities—e.g., Python's Hypothesis framework [37] had an estimated 500K users in 2021 according to a JetBrains survey [32]. Still, there is plenty of

30 OCaml developers interviewed on their use of PBT



Why should we care?

1. Testing observational equivalence requires significant programmer effort

- Developers described this process as "tedious" & "overwhelming"
- High "overhead" associated with writing PBT boilerplate

Goldstein et al. (ICSE '24)

in languages like OCaml with rich module structures, researchers should aim to increase automation around differential testing and produce a test harness for comparing modules without requiring any manual setup

Why should we care?

2. Large OCaml software systems are built using multiple modules that implement the same signature



MirageOS



Module type	Implementations
Mirage_kv.R0	Crunch, Kv_Mem, Kv_unix,
	Mirage_tar, XenStore,
	Irmin, Filesystems
Mirage_kv.RW	Wodan
Mirage_fs.S	Fat, Git, Fs_Mem, Fs_unix
Mirage_net.S	tuntap, vmnet, rawlink
ARP, IP, UDP, TCP	IPV4, IPV6, Qubesdb_IP,
	Udp, Updv4_socket, Tcp,
	Tcpv4_socket,
STACK	Direct Socket Oubos
STACK	Direct, Socket, Qubes, Static IP, With DHCP
	Statie_ii, with_bilet
RANDOM	Stdlib, Nocrypto, Test
	- 1
HTTP	Cohttp, Httpaf
FLOW	Conduit.With_tcp,
	Conduit.With_tls
DNS, DHCP, SYSLOG	Dns, Unix, Charrua_unix,
	Charrua, Syslog. Tcp,
	Syslog.Udp, Syslog.Tls
	Jitsu, Irmin,

Radanne et al. (2019)

What if I told you ...

What if I told you ...

You can take two modules that implement the same signature ...

module type S

module M1 : S module M2 : S

What if I told you ...

You can take two modules that implement the same signature ...

module type S

module M1 : S module M2 : S

... and automatically get PBT code that compares them?

Mica

```
module type S = ...
[∂∂deriving mica]
```

```
type expr = ...

let gen_expr ty = ...

let interp = ...
```

\$ Mica: OK, passed 10000 tests.



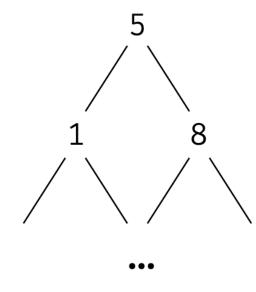


Mica automatically generates random S-operations & tests that M1, M2 are observationally equivalent w.r.t. S

module M1 : S

[1; 5; 8; ...]

module M2 : S



Mica automatically generates random S-operations & tests that M1, M2 are observationally equivalent w.r.t. S

```
module M1 : S
                                             module M2 : S
     [1; 5; 8; ...]
M1.size (M1.add 2 M1.empty) == M2.size (M2.add 2 M2.empty)
                         randomly generated
                                             M2.is_empty (...)
   M1.is_empty (...)
```

Types

(to be explained later)

expr

ty

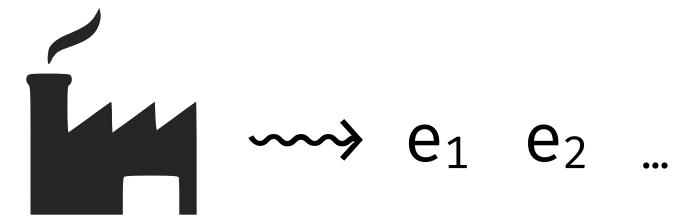
value

Types

(to be explained later)

QuickCheck Generator

expr ty value



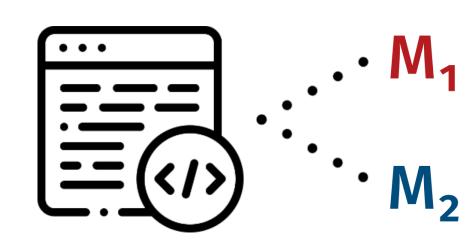
Types

(to be explained later)

expr ty value QuickCheck Generator

 $e_1 e_2 \dots$

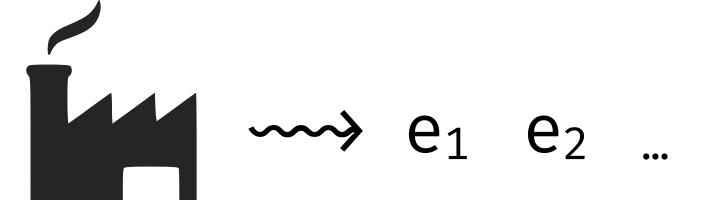
Interpreter



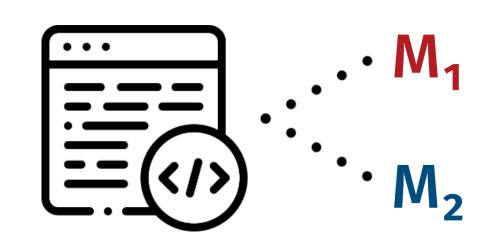
Types

(to be explained later)

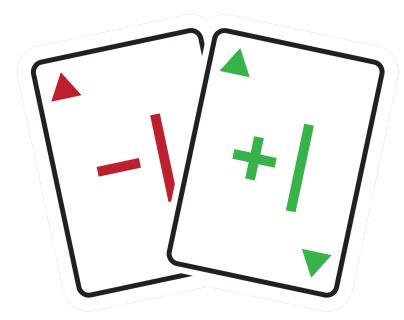
expr ty value QuickCheck Generator



Interpreter



Test Harness



Symbolic Expressions

Model operations in the module signature using an inductively-defined algebraic data type

```
module signature the expr type

type expr =

val empty : 'a t \longleftrightarrow | Empty

val is_empty : 'a t \to bool \longleftrightarrow | Is_empty of expr

val insert : 'a \to 'a t \to 'a t \longleftrightarrow | Insert of int * expr

...
```

Symbolic Expressions

Types

type ty = Int Bool T

Symbolic Expressions

Values

Interpretation Functor

```
module Interpret (M : S) = ...
```

```
expr \longrightarrow value
```

QuickCheck Generator

randomly generate symbolic representations of well-typed expressions

gen_expr : ty \rightarrow expr Generator.t

QuickCheck Generator

randomly generate symbolic representations of well-typed expressions

gen_expr : ty \rightarrow expr Generator.t

Union (Insert (2, Empty), Empty)



QuickCheck Generator

randomly generate symbolic representations of well-typed expressions

```
gen_expr : ty \rightarrow expr Generator.t
```

Union (Insert (2, Empty), Empty) Is_empty (Size Empty)





Test Harness Functor

Checks observational equivalence at <u>concrete</u> types

module TestHarness (M1 : S) (M2 : S) =
$$\dots$$

int 'a t



Observational equivalence is only well-defined for <u>concrete</u> types

Observational equivalence is only well-defined for <u>concrete</u> types

Concrete types

(Defined *only* in terms of primitive types, polymorphic equality works!)

int

string list

char * bool

Can be compared directly



Observational equivalence is only well-defined for <u>concrete</u> types

Concrete types

(Defined *only* in terms of primitive types, polymorphic equality works!)

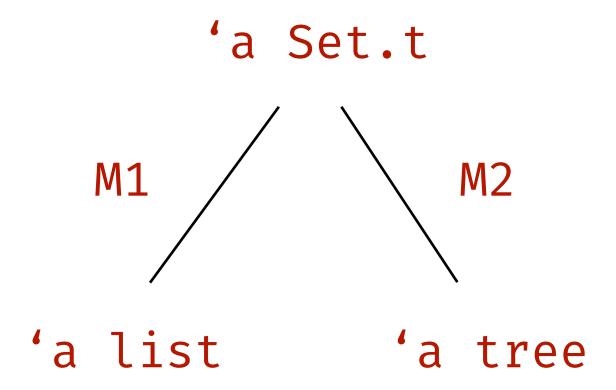
int
string list
char * bool

Can be compared directly



Abstract types

(Definition is hidden, abstract notion of equality)



Can't be compared directly



Type-Directed Observational Equivalence

Mica checks for equivalence at all unique <u>concrete</u> types which appear as the return types of functions in S

```
module type S = sig

type 'a t

val member : 'a \rightarrow 'a t \rightarrow bool

val size : 'a t \rightarrow int

...

end
```

Type-Directed Observational Equivalence

Mica checks for equivalence at all unique <u>concrete</u> types which appear as the return types of functions in S

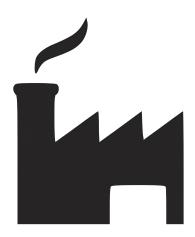
```
module type S = sig
  type 'a t
  val member : 'a \rightarrow 'a t \rightarrow bool
  val size : 'a t \rightarrow int
...
end
```

the results of <u>observation functions</u>
(clients of S can only *observe* discrepancies
between M1 & M2's behavior by calling these functions)

QuickCheck Generator

Generates *random* symbolic expressions

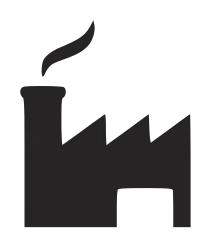
```
(Size
(Union (Add 2 Empty) ...)
```



QuickCheck Generator

Generates *random* symbolic expressions

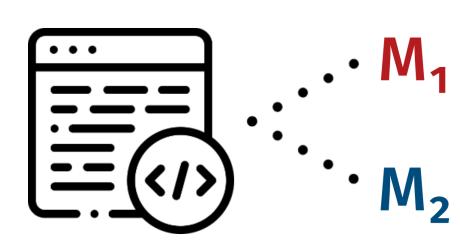
```
(Size
(Union (Add 2 Empty) ...)
```



Interpreter

Interprets expressions over modules

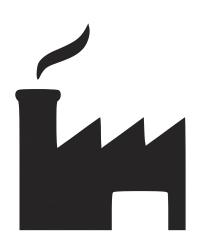
```
M.size
(M.union (M.add 2 M.empty) ...)
```



QuickCheck Generator

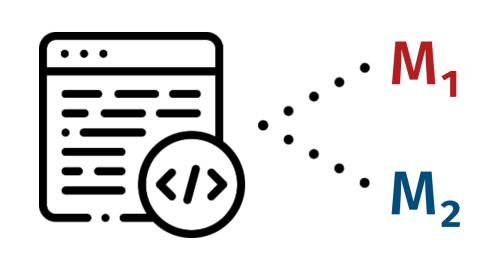
Generates *random* symbolic expressions

```
(Size
(Union (Add 2 Empty) ...)
```



Interpreter

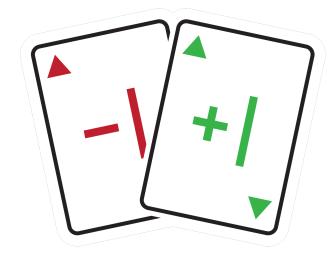
Interprets expressions over modules



Test Harness

Checks observational equivalence

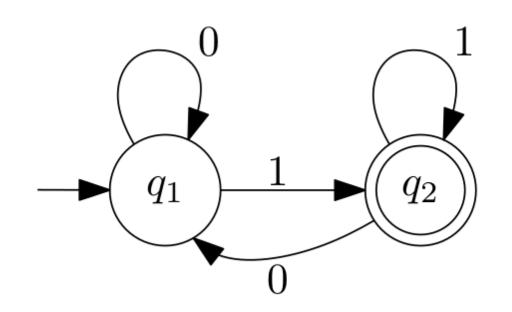
$$v1 = ? v2$$



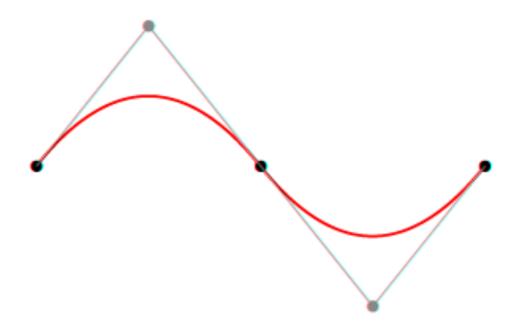
Case Studies

Case Studies

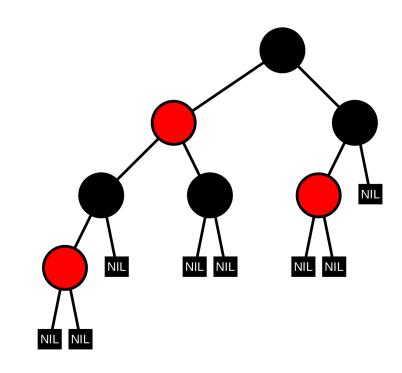
Regex Matchers



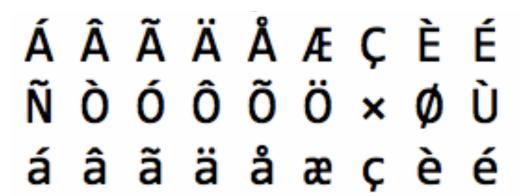
Polynomials



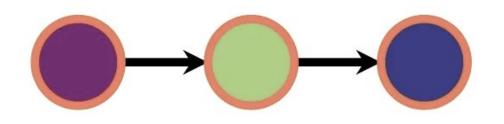
Persistent Maps



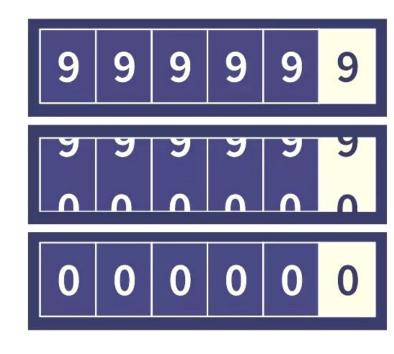
Character Sets



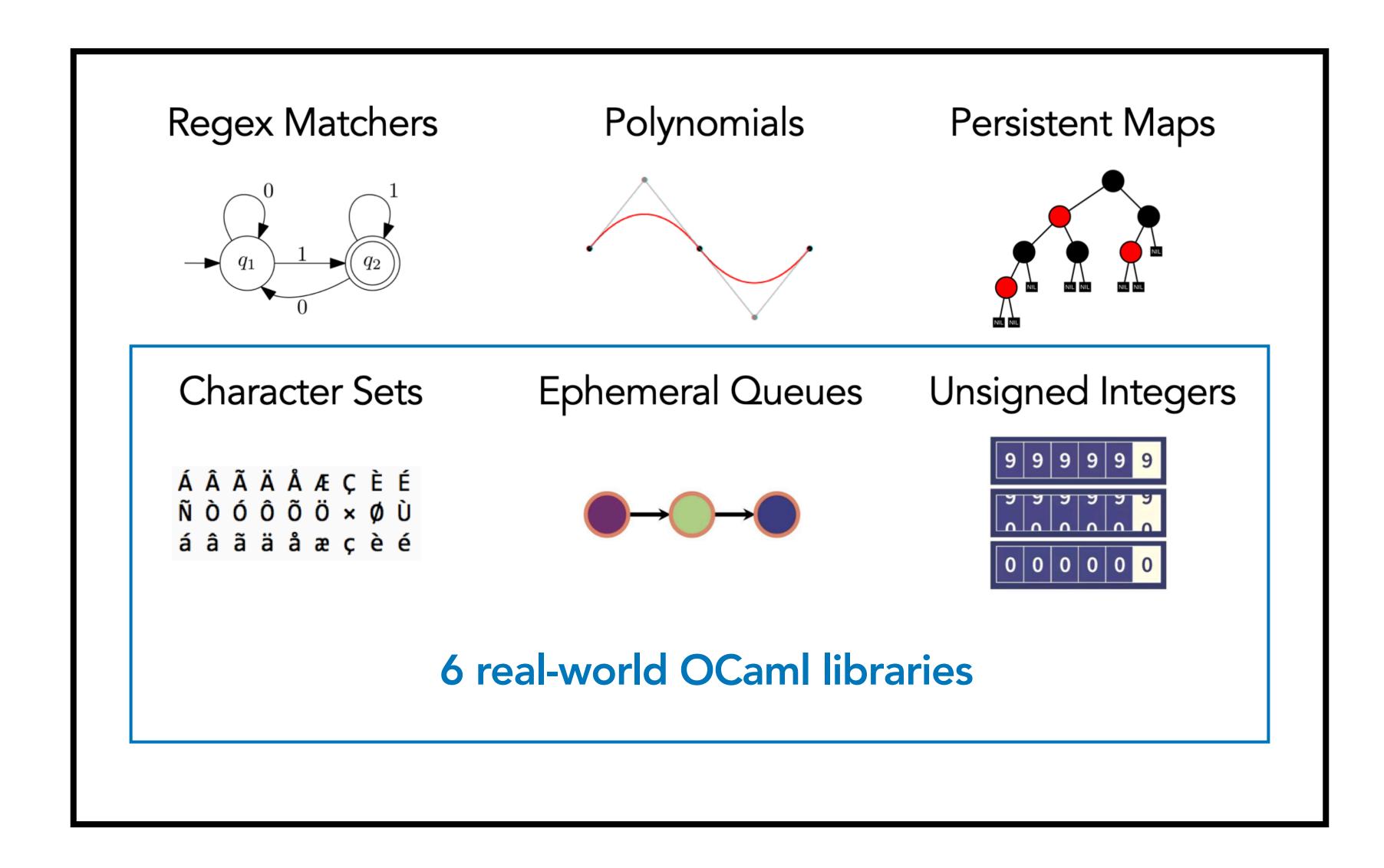
Ephemeral Queues



Unsigned Integers



35 manually-inserted bugs caught



Case study: How to Specify It

John Hughes



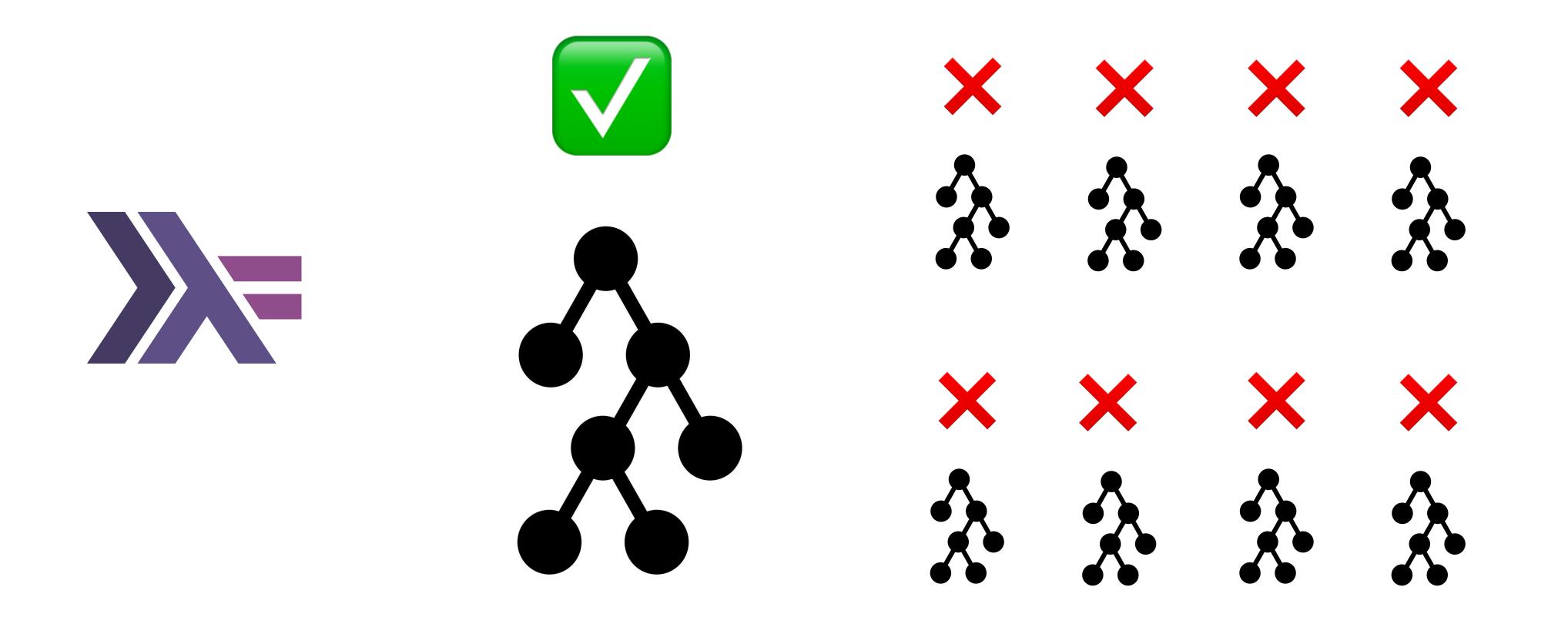
How to Specify it!

A Guide to Writing Properties of Pure Functions.

(TFP '19)

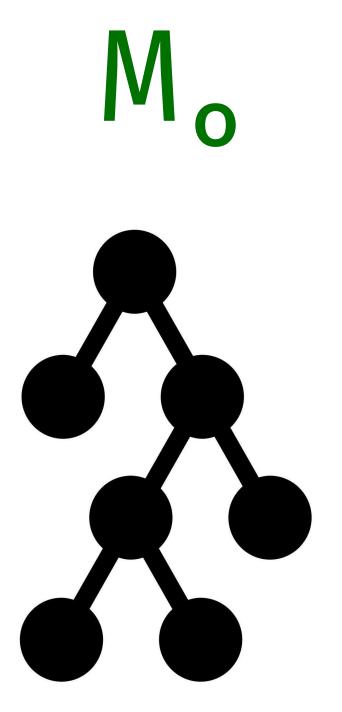


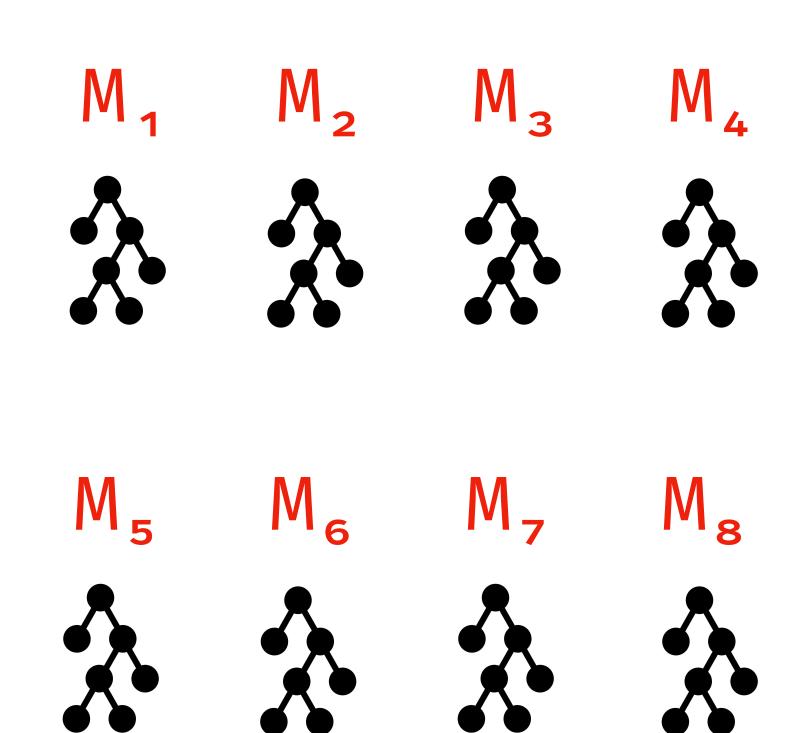
Case study: BSTs done 9 ways



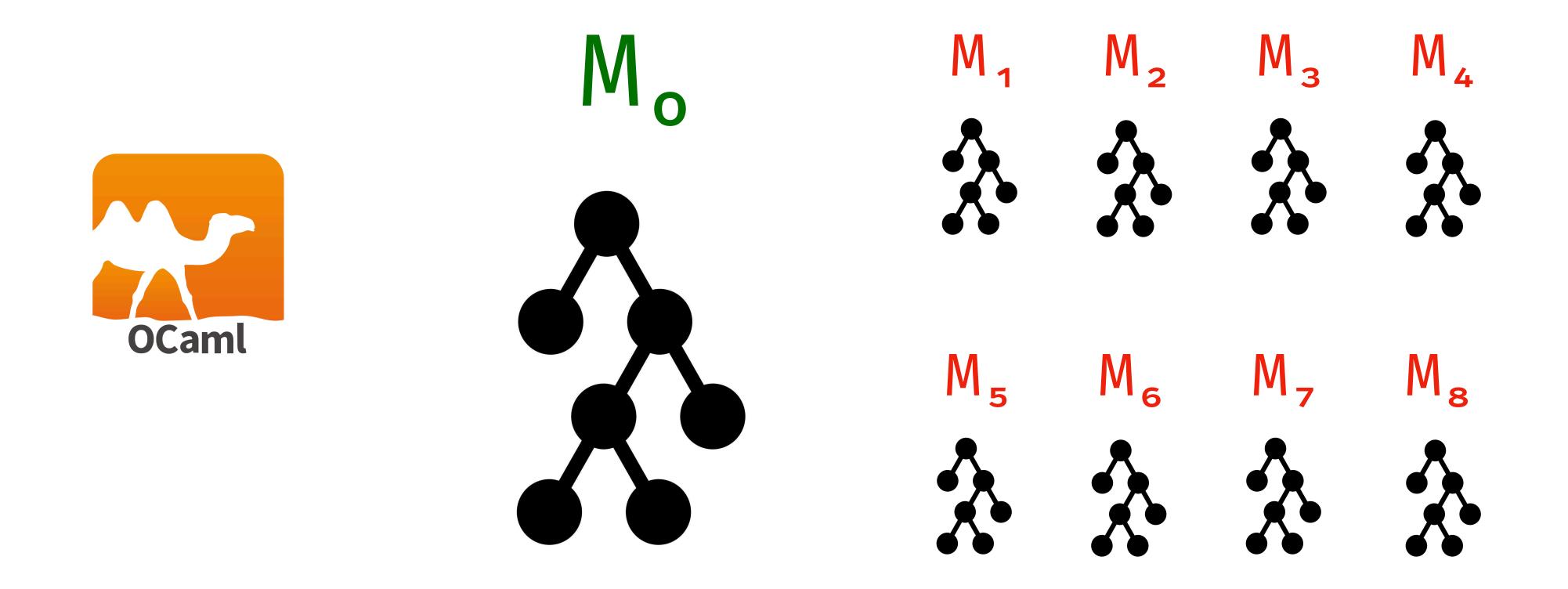
Case study: BSTs done 9 ways







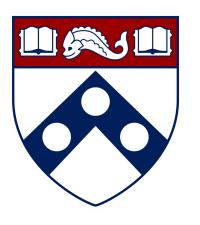
Case study: BSTs done 9 ways



Each bug caught within ~170 randomly generated symbolic expressions

Case study: Finding bugs in student assignments

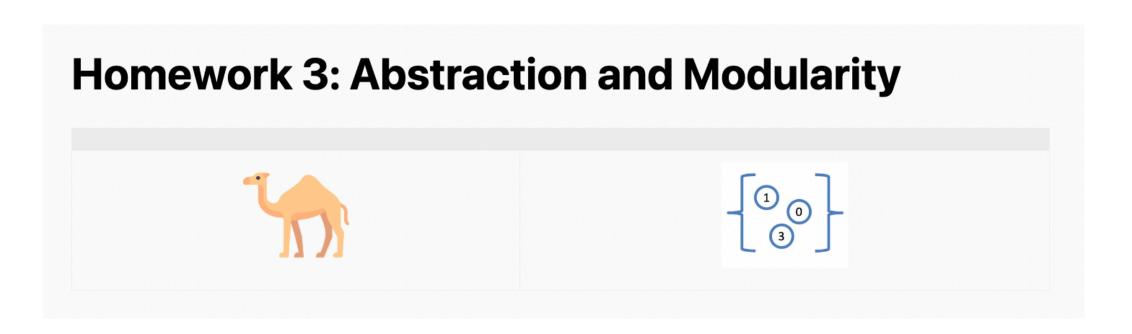






- Penn's undergrad intro OCaml class
 - 400 students every semester
- Natural source of bugs!

Case study: Sets done 400 ways



Penn CIS 1200, Fall 2023

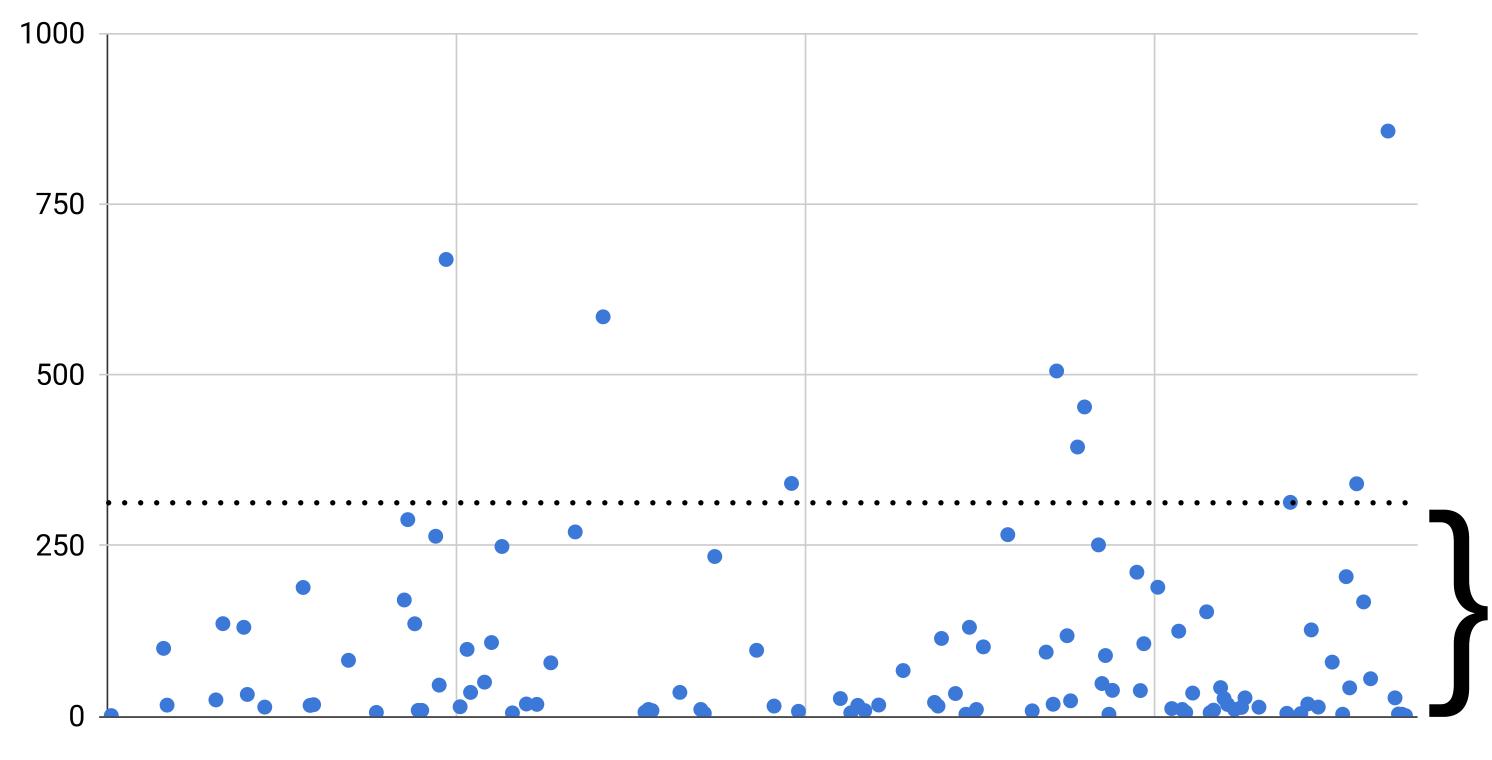
As homework, students were asked to implement sets using lists & BSTs

(we looked at historical data from Fall '23)

Are students' implementations observationally equivalent?

Mica caught bugs in 107 students' submissions! (29% of the class)

Average no. of random inputs required to catch bug



91% of bugs caught within 300 randomly generated symbolic expressions!

(each dot represents a student, lower is better)

VS Code Integration with Tyche

Goldstein et al. (to appear at UIST '24)

TYCHE: Making Sense of Property-Based Testing Effectiveness

Harrison Goldstein

University of Pennsylvania Philadelphia, PA, USA hgo@seas.upenn.edu

Jeffrey Tao

University of Pennsylvania Philadelphia, PA, USA jefftao@seas.upenn.edu

Zac Hatfield-Dodds*

Anthropic San Francisco, CA, USA zac.hatfield.dodds@gmail.com

Benjamin C. Pierce

University of Pennsylvania Philadelphia, PA, USA bcpierce@seas.upenn.edu

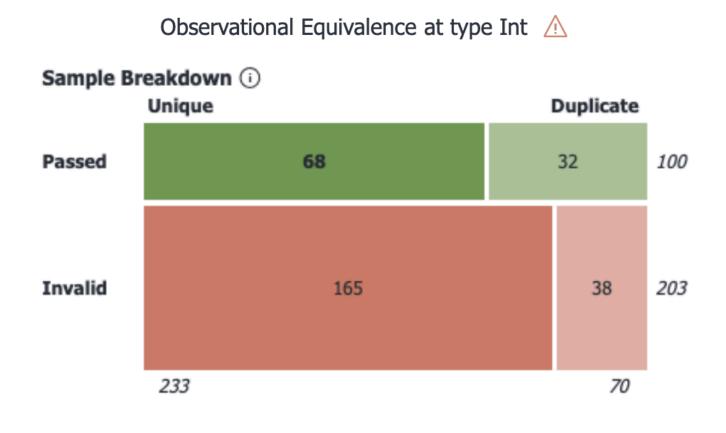
Andrew Head

University of Pennsylvania Philadelphia, PA, USA head@seas.upenn.edu

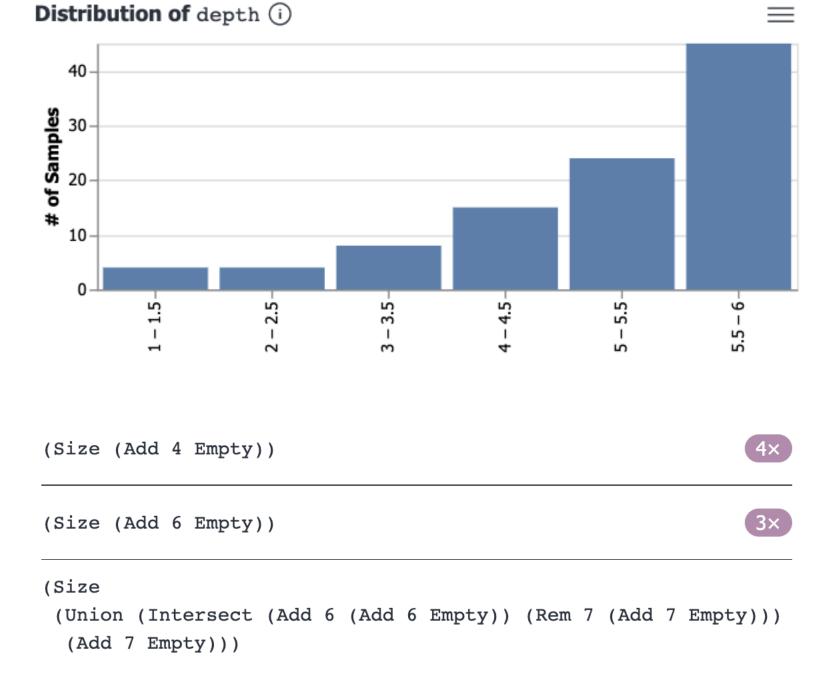
Tyche Harrison Goldstein | ≟ 226 installs | ★★★★★ A VSCode extension for visualizing data produced when testing a Hypothesis property. Install

Using Tyche to display Mica's test results

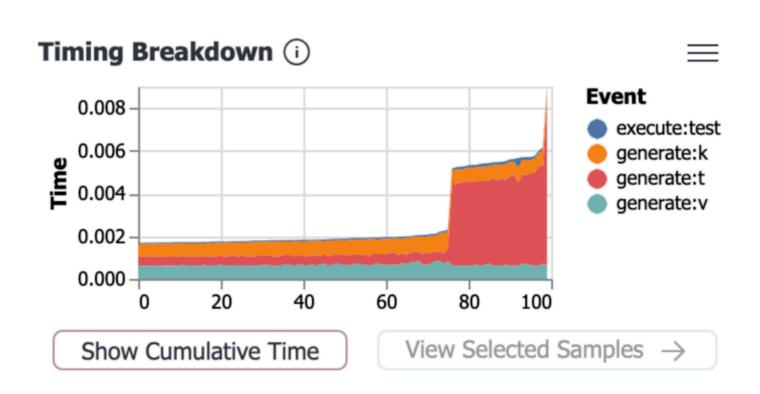
Observational equivalence test results



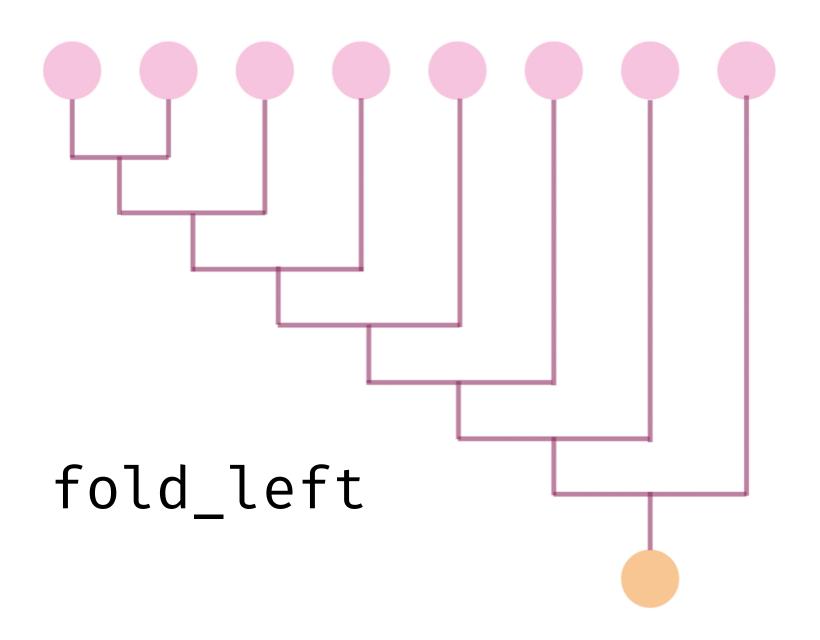
Distribution of symbolic expressions



Timing information



Support more higher-order functions



Support imperative code



Graphic from Ahrefs

```
type expr = ...
  | Seq of expr * expr

Seq (e1, e2) == e1; e2
```

Support differential testing of functors

```
module F (M1 : S1) ... (Mn : Sn) = ...
```

module
$$G$$
 (N1 : S1) ... (Nn : Sn) = ...

Use coverage-guided fuzzing to guide Mica's QuickCheck generator

Crowbar (OCaml '17)

Jane Street

FuzzChick (OOPSLA '19)



ParaFuzz (OCaml '21)



Mica is:

a PPX extension

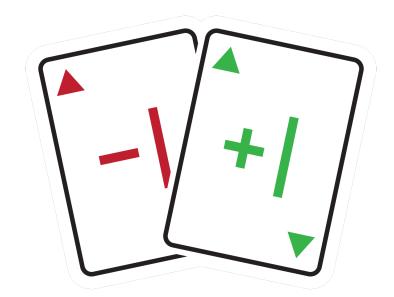
[aaderiving mica]

that **automatically** derives

PBT code



for testing module observational equivalence



Trying out Mica

Installation

opam install ppx_mica



Contributions welcome!

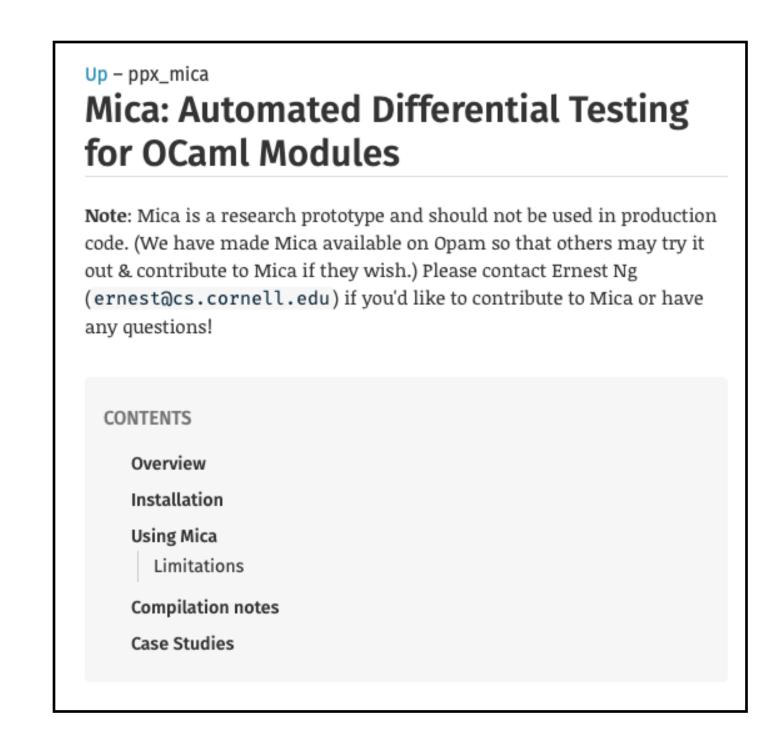
Web Demo

(Displays code produced by Mica)



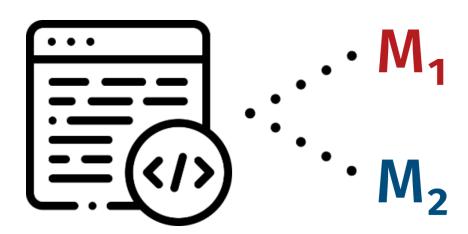
Docs

ngernest.github.io/mica



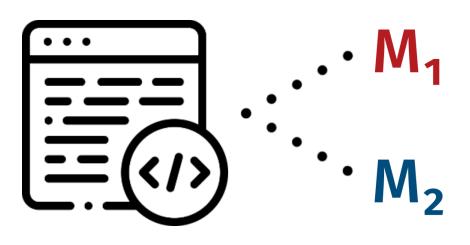
PPX Extension

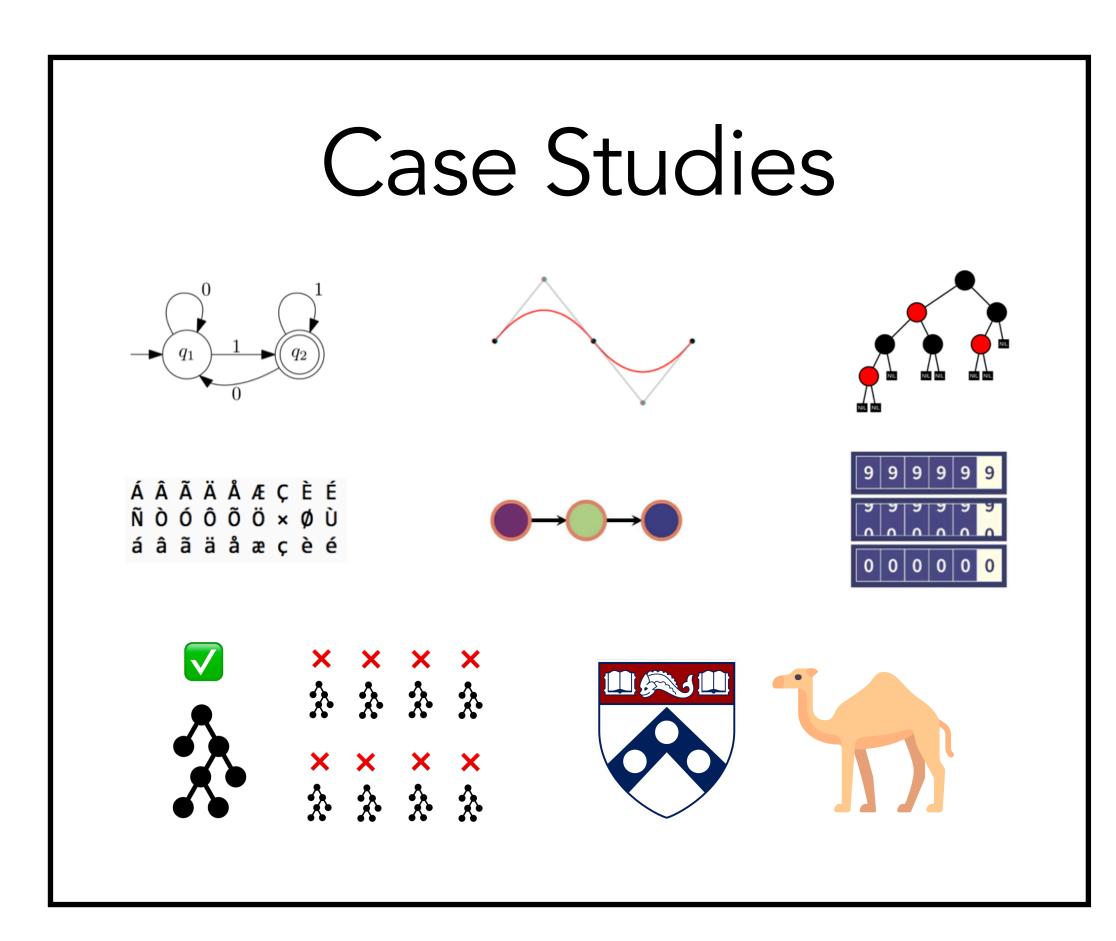




PPX Extension



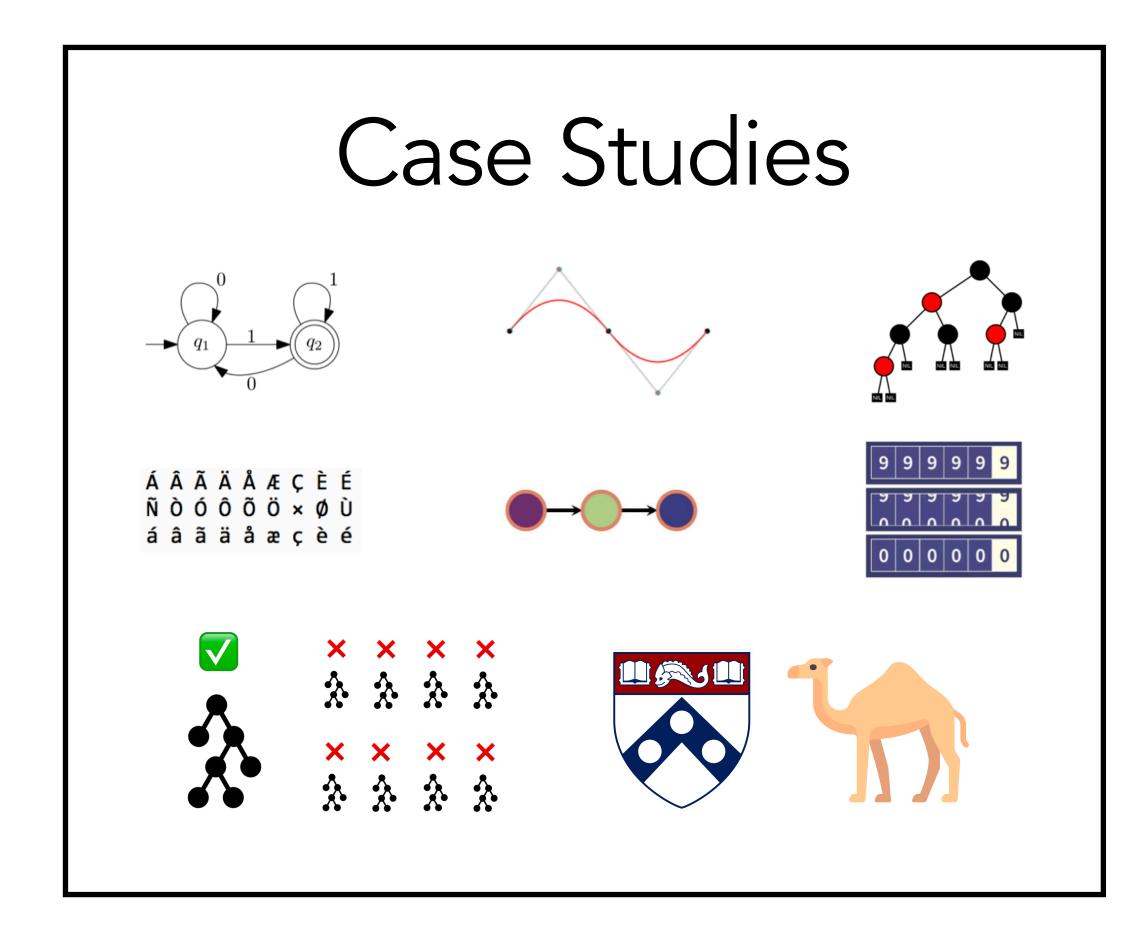


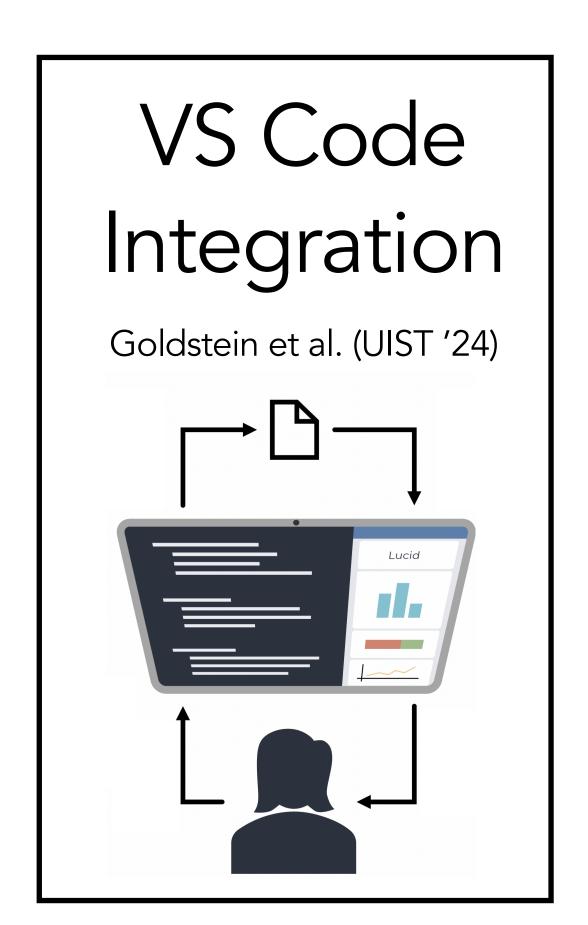


PPX Extension

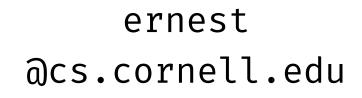




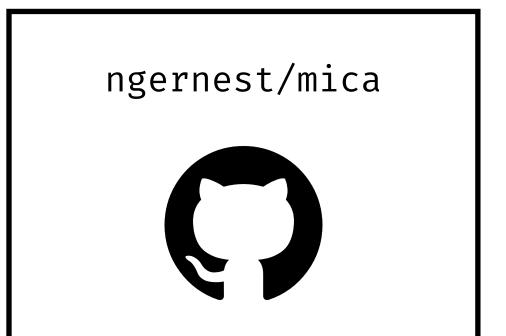


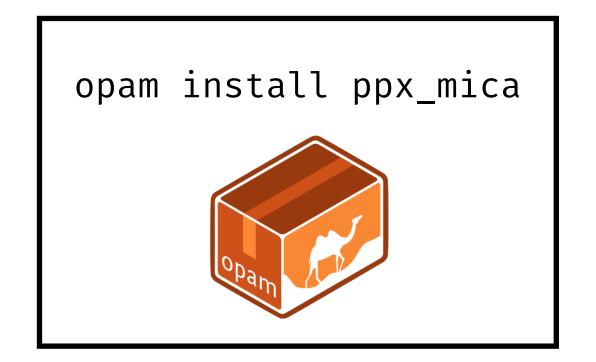


Thanks!



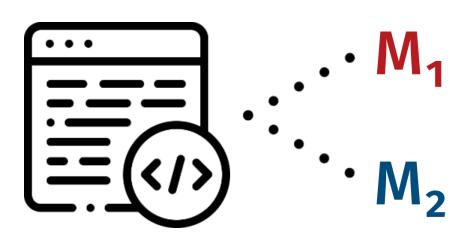


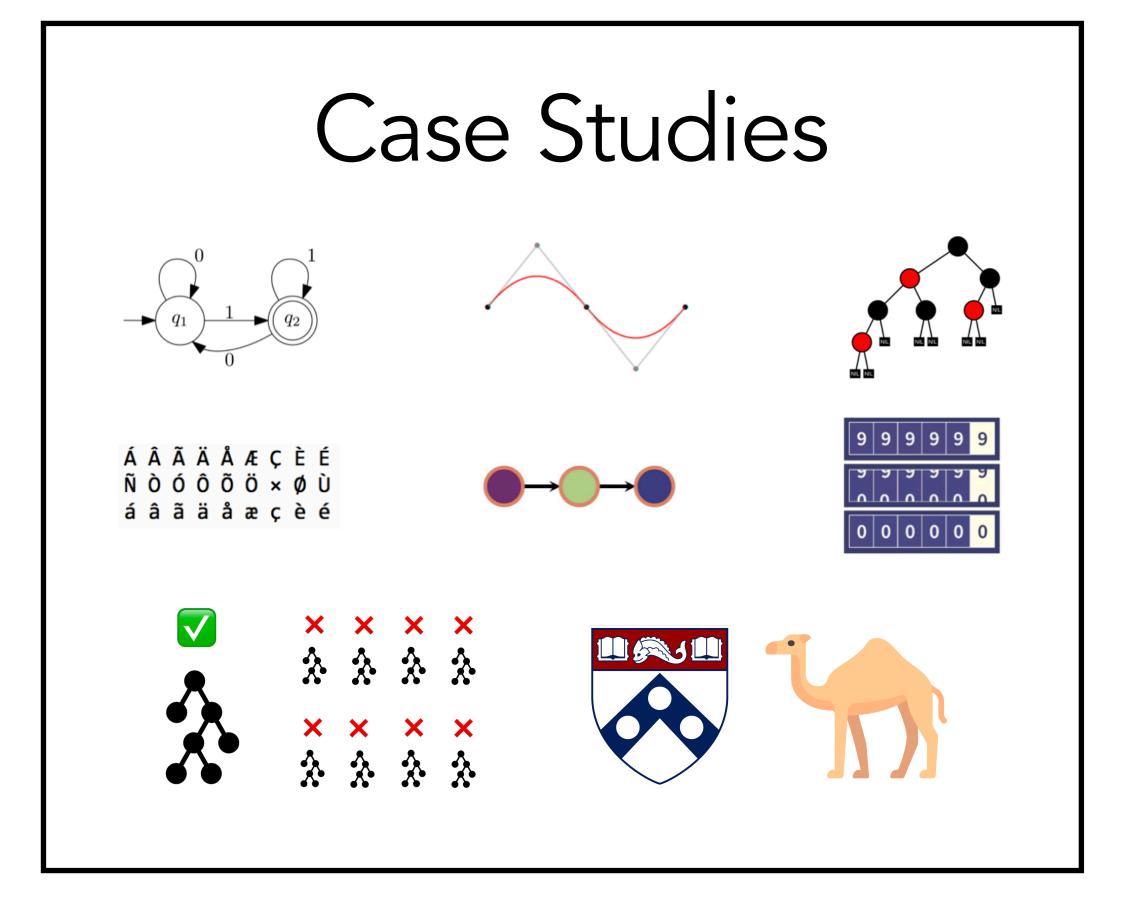


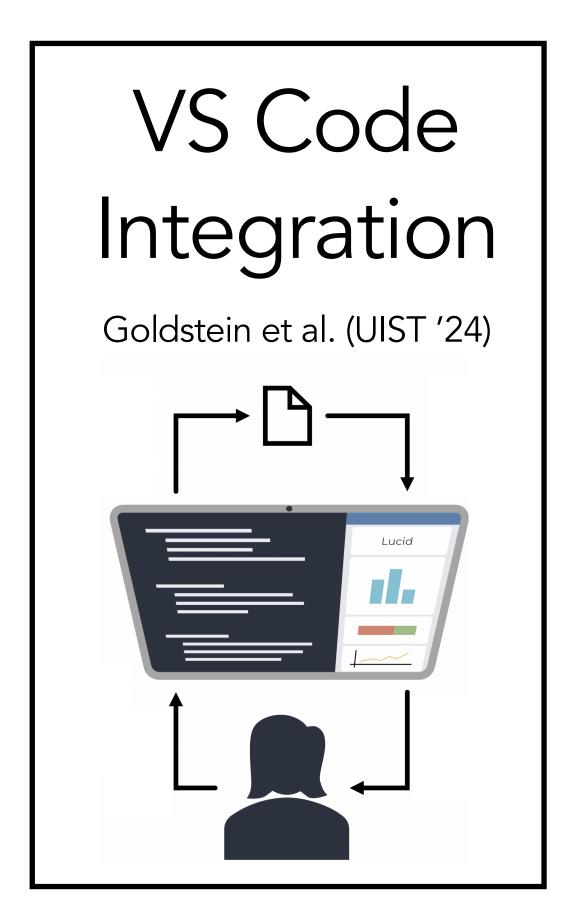












Appendix: extrinsic vs intrinsic typing

Some frequently asked questions

Why are Mica's symbolic expressions *extrinsically* typed, and not *intrinsically* typed?

Why do you have exprand not 'a expr?

Extrinsic

Symbolic expressions: Algebraic data type

Terms and types defined separately

(It is possible to construct representations of ill-typed terms!)

Auxiliary value type needed for interpreter

interp :
$$expr \rightarrow value$$

Intrinsic

Symbolic expressions: Parameterized GADT

Terms & types are intertwined

(By construction, only representations of well-typed terms are allowed)

No auxiliary value type needed

interp : 'a expr
$$\rightarrow$$
 'a

So why not use intrinsic typing instead?

Well, it is possible to write an intrinsically-typed interpreter for symbolic expressions ...

```
module Interpret (M : S) = struct
  (** Both [value] & [expr] are now GADTs *)
  type _ value = ...
  type _ expr = ...

(** [a] is a locally abstract type - [a] is instantiated
      w/ different concrete types in the function body *)
  let eval_value (type a) (v : a value) : a = ...

(** [interp] uses polymorphic recursion *)
  let rec interp : type a. a expr → a = ...
```

Intrinsic typing is non-trivial

In OCaml, writing a QuickCheck generator for random inhabitants of GADTs is hard

Intrinsic typing is non-trivial

It is slightly easier in Haskell, but requires existential types & higher-kinded polymorphism

```
-- an existential type
- `f` is a type constructor of kind `* → *`
data Some f where
Exists :: f t → Some f
```

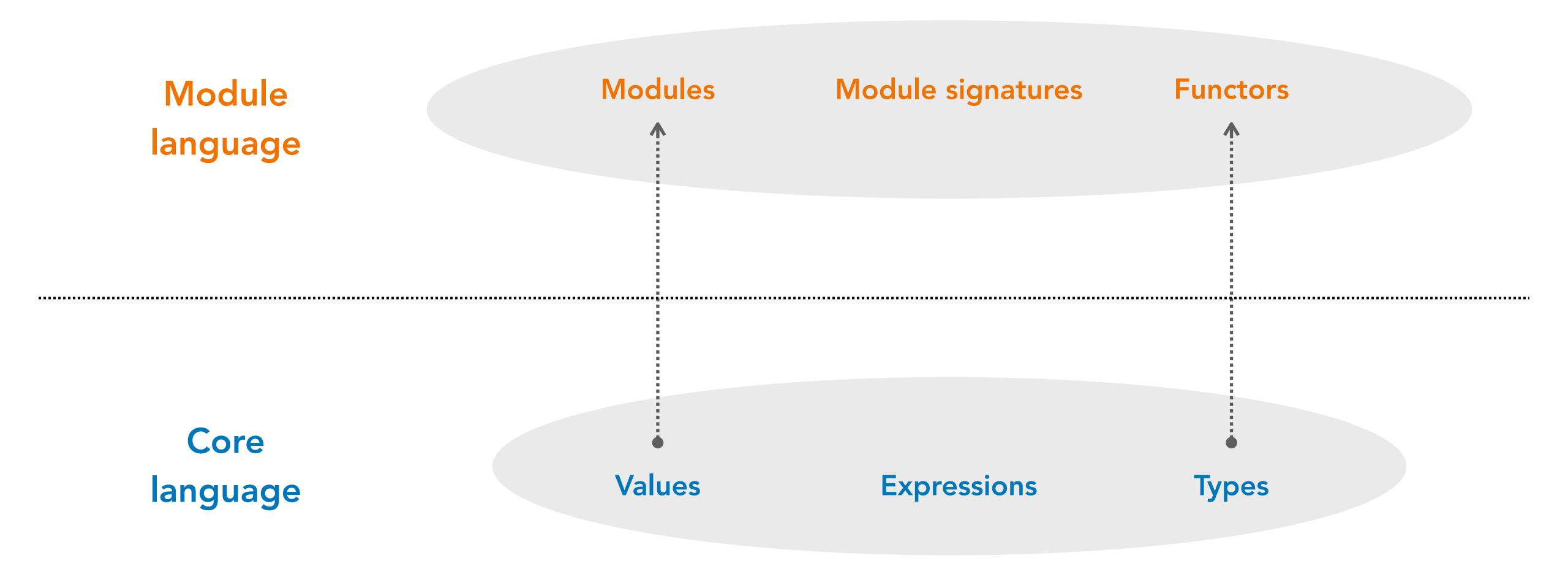
(idea due to Stephanie Weirich)

Why we used extrinsic typing

- Extrinsic typing is simpler & easier to get right
- Mica needs to derive property-based testing code automatically, for *any* possible module signature it might encounter

Other Appendix Slides

"OCaml is two languages in one"



Monomorphization

Heuristic: 'a →→ int

Further reading:

Testing Polymorphic Properties

Jean-Philippe Bernardy, Patrik Jansson, and Koen Claessen

Chalmers University of Technology {bernardy,patrikj,koen}@chalmers.se

ESOP 2010

Logarithm and Program Testing

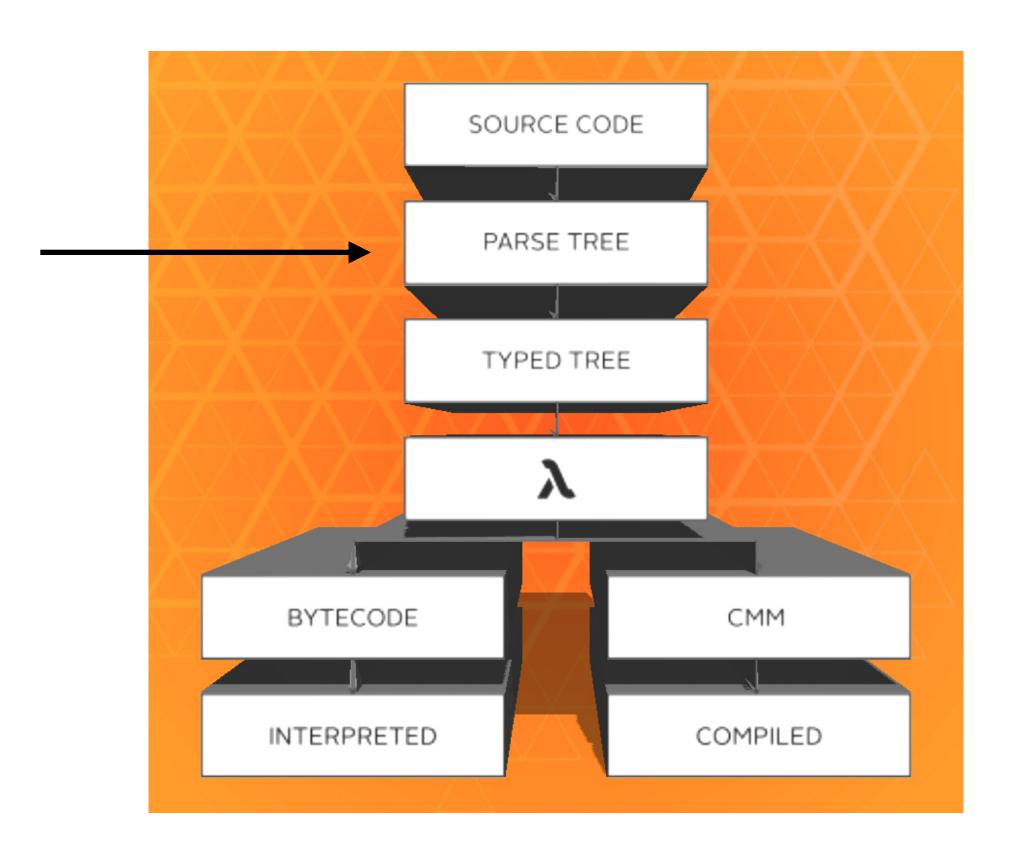
KUEN-BANG HOU (FAVONIA), University of Minnesota, USA ZHUYANG WANG, University of Minnesota, USA

Randomized property-based testing has gained much attention recently, be at polymorphic properties. Although Bernardy *et al.* have developed a the polymorphic properties to monomorphic ones, it relies upon ad-hoc embedding-projection to a particular form. This paper skips the embedding-projection

POPL 2022

PPXes (PreProcessor Extensions)

- Preprocessors that operate on the untyped AST (Parsetree) produced by the OCaml compiler
- PPX derivers = ast_node \rightarrow ast_node functions
- Similar facilities exist in Haskell / Rust



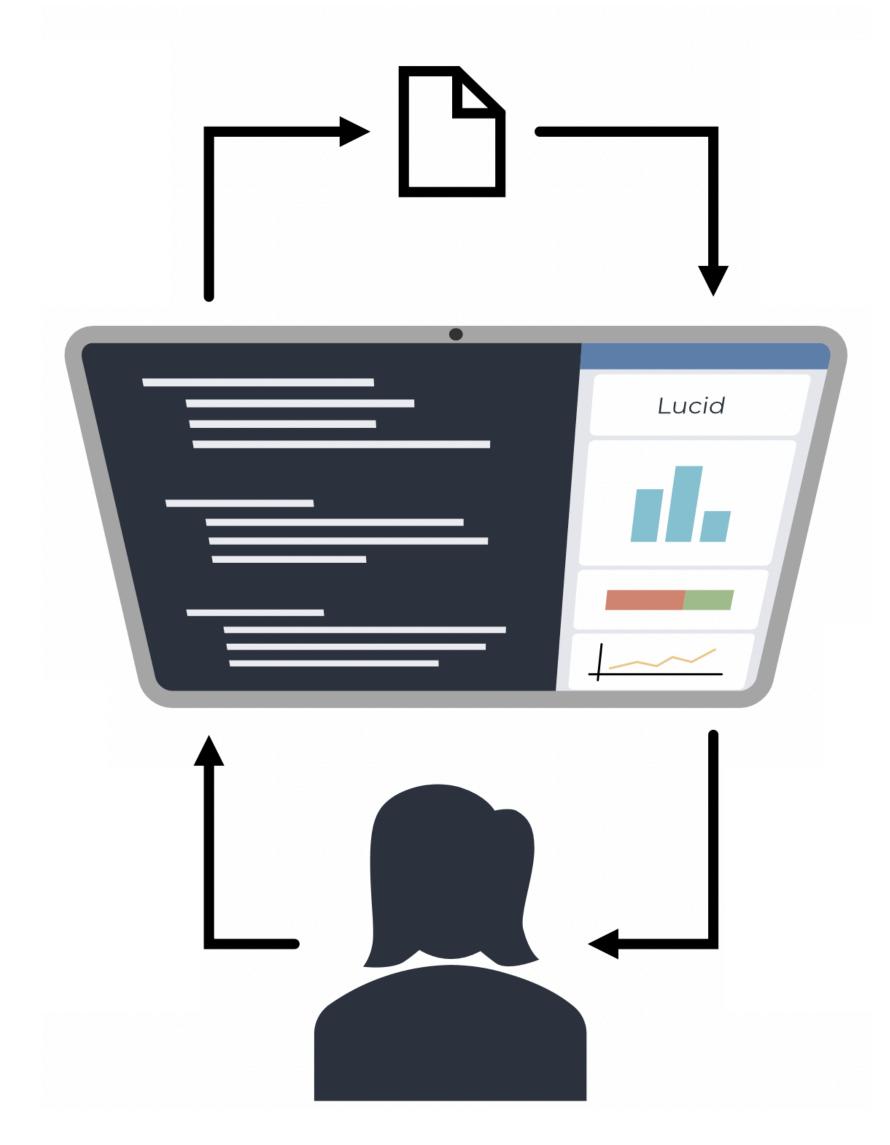
Interacting with Mica + Tyche

Annotate module signature
 & invoke Mica test harness

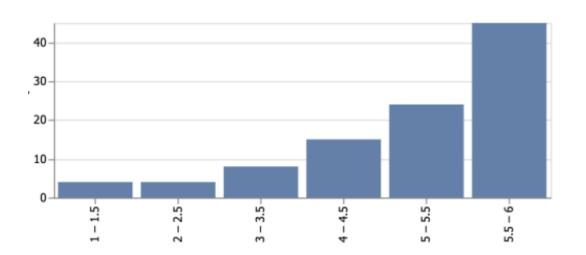
```
module type S = ...
[@@deriving mica]
```

4. Update module implementations

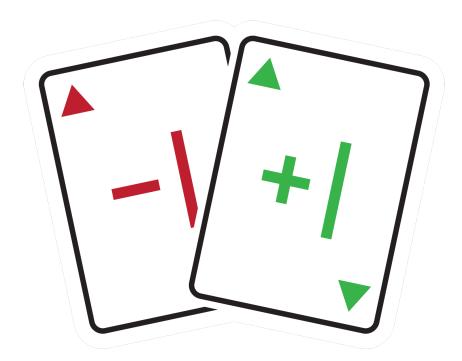
```
module M1 : S = ...
module M2 : S = ...
```



2. Tyche visualizes test statistics



3. Examine test results



Representing Higher-Order Functions Using Symbolic Expressions

map: ('a
$$\rightarrow$$
 'b) \rightarrow 'a t \rightarrow 'b t

type expr =
$$Map$$
 of (int \rightarrow int) * expr | ...

Shrinking and Showing Functions (Functional Pearl)

Koen Claessen

Chalmers University of Technology koen@chalmers.se

Haskell Symposium 2012

Generating Well-Typed Terms That Are Not "Useless"

JUSTIN FRANK, University of Maryland, USA
BENJAMIN QUIRING, University of Maryland, USA
LEONIDAS LAMPROPOULOS, University of Maryland, USA

Random generation of well-typed terms lies at the core of effective random testing of compilers for languages. Existing techniques have had success following a top-down type-oriented approach to that makes choices locally, which suffers from an inherent limitation: the type of an expressi generated independently from the expression itself. Such generation frequently yields functions with types that cannot be used to produce a result in a meaningful way, leaving those arguments un "use-less" functions can hinder both performance, as the argument generation code is dead but st

POPL 2024

Supporting other PBT libraries besides Core.Quickcheck

- Mica's design is *library-agnostic*: developers can write other backends that support other OCaml PBT libraries (e.g. QCheck, Crowbar, ...)
 - (We picked Core.Quickcheck just because we were most familiar with it)
- It'd be interesting to build on recent work extending **Etna** (an evaluation platform for different PBT frameworks) for comparing the efficacy of different OCaml PBT libraries

ETNA: An Evaluation Platform for Property-Based Testing (Experience Report)

JESSICA SHI, University of Pennsylvania, USA
ALPEREN KELES, University of Maryland, USA
HARRISON GOLDSTEIN, University of Pennsylvania, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
LEONIDAS LAMPROPOULOS, University of Maryland, USA

ICFP 2023

Evaluating PBT Frameworks in OCaml

ABSTRACT

Property-based testing (PBT) is an effective way of finding bugs in programs by automatically generating test cases to check user-defined properties. It is especially powerful for testing functional codebases, where it exploits immutability, purity, and the strong typing information available. Although the PBT space contains a wide variety of frameworks with a plethora of approaches to generating inputs, there is a lack of tools that compare the effectiveness of the frameworks. One such tool, ETNA [6], was recently presented to empirically evaluate and compare PBT techniques

properties should only apply to valid BSTs, not arbitrary binary trees. A simple solution is to follow the data definition of the tree type to create an arbitrary binary tree, and then filter out those that are not valid BSTs. Shi et al. [6] call this approach *type-based*, as the generation of the test cases is guided by the type definition. However, as the workload becomes more and more sophisticated, this filtering approach falls apart. The chance of a random tree being a valid red-black tree is far smaller. The chance of a random lambda calculus expression being type-correct is even lower. This issue gives rise to *bespoke* generators, designed with the preconditions in mind to only generate valid test cases. As the input space grows

PLDI 2024 SRC

Compilation Times + How long it takes Mica's tests to run

In practice, we haven't found compilation / test runtimes to be an issue!

Module Signature	Compilation Times (using a Mica prototype)	Runtime of PBT test harness
Sets	309.25 µs	2.55 ns
Stacks	361.08 µs	2.54 ns
Polynomials	302.82 µs	2.57 ns
Maps	262.84 µs	2.56 ns
Regexes	266.61 μs	2.57 ns

(Measured using Core_bench on an M1 Mac)

How to Specify It (BST Case Study) Stats

Bug revealed only in one branch of a pattern-match: coverage information would help us here!

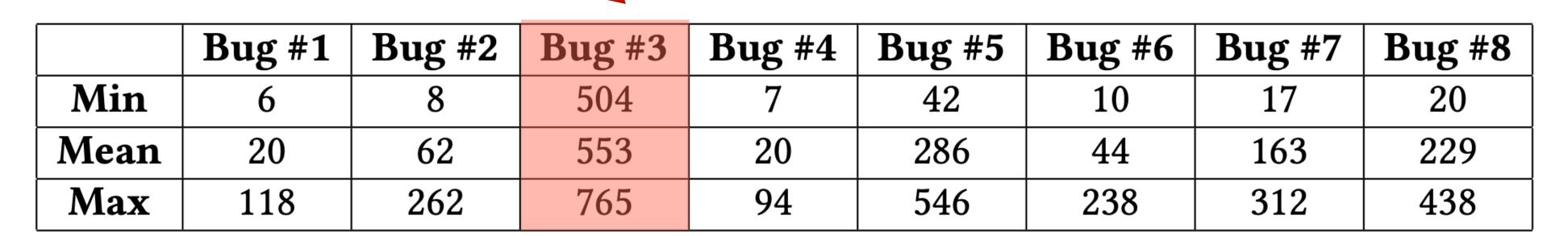


Fig. 3. Average mean no. of trials required to provoke failure in an observational equivalence test

Invoking QuickCheck generators for opaque types

- For any user-defined type t, the user should provide a QuickCheck generator called quickcheck_generator_t
- Mica will then invoke this generator by calling the appropriate directive from ppx_quickcheck in the derived code

```
let rec gen_expr (ty : ty) : expr Generator.t =
  match ty, QC.size with
  | (T, _) → ...
  let%bind t = [%quickcheck.generator: t] in ...
```

Related Work

Monolith
(Pottier 2021)

Articheck

(Braibant et al. 2014)

- GADT-based DSLs for testing ML modules
- Mutation-based fuzzing
- Mica automatically derives the requisite PBT code

Related Work

QCSTM (Midtgaard 2020)

Model_quickcheck (Dumont 2020)

- Algebraic data types for representing symbolic expressions
- Mica adds support for binary operations on abstract types

Future Work (Engineering)

Contact us if you're interested in contributing to Mica!

- Shrinking
- Modules with multiple abstract types
- Compute "module coverage" for tests
- Support other OCaml PBT libraries

ernestacs.cornell.edu